

1.5 Laws of algebra of sets

(1) Idempotent laws: For any set A , we have

(i) $A \cup A = A$ (ii) $A \cap A = A$

(2) Identity laws: For any set A , we have

(i) $A \cup W = A$ (ii) $A \cap U = A$

i.e., W and U are identity elements for union and intersection respectively.

(3) Commutative laws: For any two sets A and B , we have

(i) $A \cup B = B \cup A$ (ii) $A \cap B = B \cap A$

(iii) $A \Delta B = B \Delta A$

i.e., union, intersection and symmetric difference of two sets are commutative.

(iv) $A - B \neq B - A$ (v) $A \times B \neq B \times A$

i.e., difference and cartesian product of two sets are not commutative

(4) Associative laws: If A , B and C are any three sets, then

(i) $(A \cup B) \cup C = A \cup (B \cup C)$ (ii) $A \cap (B \cap C) = (A \cap B) \cap C$

(iii) $(A \Delta B) \Delta C = A \Delta (B \Delta C)$

i.e., union, intersection and symmetric difference of two sets are associative.

(iv) $(A - B) - C \neq A - (B - C)$ (v) $(A \times B) \times C \neq A \times (B \times C)$

i.e., difference and cartesian product of two sets are not associative.

(5) Distributive law: If A , B and C are any three sets, then

(i) $A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$

(ii) $A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$

i.e., union and intersection are distributive over intersection and union respectively.

(iii) $A \times (B \cap C) = (A \times B) \cap (A \times C)$

(iv) $A \times (B \cup C) = (A \times B) \cup (A \times C)$

(v) $A \times (B - C) = (A \times B) - (A \times C)$

(6) De-Morgan's law: If A , B and C are any three sets, then

(i) $(A \cup B)' = A' \cap B'$

(ii) $(A \cap B)' = A' \cup B'$

(iii) $A - (B \cap C) = (A - B) \cup (A - C)$

(iv) $A - (B \cup C) = (A - B) \cap (A - C)$

(7) If A and B are any two sets, then