

CHAPTER – 15

PROBABILITY

15.1 INTRODUCTION

EXPERIMENT:

The word experiment means an operation, which can produce well defined outcomes. There are two types of experiment:

- (i) Deterministic experiment (ii) Probabilistic or Random experiment

(i) **Deterministic Experiment:** Those experiments which when repeated under identical conditions, produced the same results or outcome are known as deterministic experiments. For example, Physics or Chemistry experiments performed under identical conditions.

(ii) **Probabilistic or Random Experiment:-** In an experiment, when repeated under identical conditions, it does not produce the same outcomes every time. For example, in tossing a coin, one is not sure that if a head or tail will be obtained. So it is a random experiment.

Sample space: The set of all possible outcomes of a random experiment is called a sample space associated with it and is generally denoted by S. For example, When a dice is tossed then $S = \{1, 2, 3, 4, 5, 6\}$.

Event: A subset of sample space associated with a random experiment is called an event. For example, In tossing a dice getting an even no is an event.

Favorable Event: Let S be a sample space associated with a random experiment and A be an event associated with the random experiment. The elementary events belonging to A are known as favorable events to the event A. For example, in throwing a pair of dice, A is defined by "Getting 8 as the sum". Then following elementary events are as outcomes: (2, 6), (3, 5), (4, 4), (5, 3), (6, 2). So, there are 5 elementary events favorable to event A.

PROBABILITY:

If there are n elementary events associated with a random experiment and m of them are favorable to an event A, then the probability of happening or occurrence of event A is denoted by P(A)

$$\text{Thus, } P(A) = \frac{\text{Total number of favourable outcomes}}{\text{Total number of possible outcomes}} = \frac{m}{n}$$

$$\text{And } 0 \leq P(A) \leq 1$$

If, $P(A) = 0$, then A is called impossible event

If, $P(A) = 1$, then A is called sure event

$$P(A) + P(\bar{A}) = 1$$

Where $P(A)$ = probability of occurrence of A.

$P(\bar{A})$ = probability of non-occurrence of A.